Evaluating Airborne Remote Sensing ET estimates using Eddy Covariance Systems and a Heat Flux Source Area Function

José L. Chávez1, 2, †, Terry A. Howell2, †, Prasanna H. Gowda2, †, Christopher M.U. Neale2, †*, Paul D. Colaizzi2, †

†Conservation and Production Research Laboratory
USDA-Agricultural Research Service
P.O. Drawer 10, Bushland, TX 79012-0010

*Biological and Irrigation Engineering
Utah State University, Logan, UT

Abstract

Growth of population, agriculture, and industry are increasing the demand for water. As competition for water increases, use of water for production of crops must become more efficient. Thus, saving water by managing irrigation systems better may be possible if irrigation scheduling is improved by accurately estimating spatially distributed actual evapotranspiration (ET). ET can be estimated using energy balance algorithms that use agrometeorological and remote sensed surface reflectance/temperature data. In this study, the objective was to evaluate spatial ET estimates obtained with a modified energy balance-based Two Source Model (TSM). For this purpose, two high-resolution aircraft images acquired during the 2008 Bushland Evapotranspiration and Agricultural Remote Sensing Experiment (BEAREX08) at the USDA-ARS Conservation and Production Research Laboratory, Bushland, TX, were used. Predicted ET values for cotton fields were compared with measured ET from eddy covariance systems using a heat flux source area function. Results showed that the TSM slightly under estimated ET by 0.5 mm d⁻¹, (or -5.1%) with a standard deviation of 0.6 mm d⁻¹. Overall, the modified TSM performed well for LAI values less than 1.5 m² m⁻². Further research will test the modified TSM for cotton LAI values larger than 3 m² m⁻².

Keywords: Southern High Plains, semi-arid environment, remote sensing, two source energy balance model, water management.

† Corresponding author, email: jose.chavez@ars.usda.gov
2 Agricultural Engineer, Agricultural Engineer and Research Leader, Agricultural Engineer, Agricultural Engineer and Agricultural Engineer respectively.
Introduction

Remote sensing (RS) derived evapotranspiration (ET) values can potentially be used as in input in irrigation scheduling and in hydrologic simulations. In addition, seasonal ET may be used to assess the overall irrigation project efficiency, provided volumes of water pumped (or diversions) had been measured, i.e. in groundwater management in arid and semiarid regions like the Southern High Plains.

Most of the RS algorithms used to estimate crop ET are based on the land surface energy balance (EB) model. These algorithms are based on the fact that ET is a change of the water state, from liquid to vapor, depending on available energy (net radiation at the surface less the energy into the ground), Su et al. (2005).

Remote sensing (RS) based surface energy balance for land provides instantaneous estimates of latent heat flux (LE) or evapotranspiration (ET); and has been recognized as a feasible method to mapping spatially distributed crop water use (Jackson, 1984).

In terms of remote sensing based EB models, there are several algorithms available in the literature. Gowda et al. (2008) present a description and discussion on most of the EB models that use remote sensing inputs for agricultural water management. Most of the EB models are single source models, e.g. SEBI (Menenti and Choudhury, 1993), SEBAL (Bastiaanssen et al., 1998), SEBS (Su, 2002), METRIC (Allen et al., 2007), etc. These models estimate different components of the EB assuming that the surface heat fluxes
originate from a source that is the composite of vegetation and background soil (substrate).

However, there is a fundamental problem in representing a heterogeneous (sparse, non-uniform) surface as a single layer or source because of the significant influence of the soil/substrate on the total surface EB. Thus, the surface resistance to evaporation has lost physical meaning because it represents an unknown combination of stomatal resistance of the vegetation and resistance to soil evaporation (Blyth and Harding, 1995). This resulted in the development of two-source approaches or models (TSM), where the energy exchanges of the soil/substrate and vegetation are evaluated separately (Shuttleworth and Wallace, 1985); i.e. more physically based models that differentiate or partition the EB terms, $R_n$, $H$, and $LE$ between the soil and the vegetation canopy, Norman et al. (1995).

Norman et al. (1995) and Kustas and Norman (1999, 2000) developed operational methodology to the two-source approach proposed by Shuttleworth and Wallace (1985) and Shuttleworth and Guerney (1990). Their model showed good agreement with observations (made with meteorological flux stations, eddy covariance/Bowen ration EB systems) over sub-humid prairie, semi-arid shrub, and fully irrigated crops. The TSM methodology generally does not require additional meteorological or information over single-source models; however, it requires some assumptions such as the partitioning of composite radiometric surface temperature into soil and vegetation components, turbulent exchange of mass and energy at the soil level, and coupling/decoupling of energy exchange
between vegetation and substrate (i.e., parallel or series resistance networks). The energy exchange in the soil-plant-atmosphere continuum is based on resistances to heat and momentum transport, and sensible heat fluxes are estimated by the temperature gradient-resistance system. Radiometric temperatures, resistances, sensible heat fluxes, and latent heat fluxes of the canopy and soil components are derived by iterative procedures constrained by composite, directional radiometric surface temperature, vegetation cover fraction, and maximum potential latent heat flux.

In an evaluation study, Chávez et al. (2008) found out that the Norman et al. (1995) and Kustas and Norman (1999) TSM algorithm for low biomass (Leaf area index, LAI, less than 3 m\(^2\) m\(^{-2}\)) resulted in large under predictions of ET. They added that the ensemble sensible heat flux was better estimated when the surface aerodynamic resistance term was eliminated from the sensible heat flux originating from the ground, in the parallel resistance network model.

Regarding the evaluation of ET estimated using remote sensing imagery, as input in EB models, using measured ET by eddy covariance systems, Chávez et al. (2005) demonstrated that using heat flux source area functions (footprint models) was more appropriate than employing simple AOI (area of interest) polygons that average ET pixels upwind of the eddy covariance tower location.

In this study, a modified TSM, Chávez et al. (2008), was applied to very high spatial resolution airborne remote sensing imagery acquired over cotton fields in the Southern High Plains (SHP) to derive ET. Furthermore, spatially distributed ET pixels were weighted and integrated using a heat source area
function (footprint) for comparison to ET measured with eddy covariance systems in order to assess the performance of the modified TSM.

Materials and Methods

Study area

Field data collection and coinciding acquisition of high resolution remote sensing data was made during the 2008 cotton cropping season at the USDA-ARS Conservation and Production Research Laboratory (CPRL), located in Bushland, Texas. The geographic coordinates of the CPRL are [35° 11' N, 102° 06' W], and its elevation is 1,170 m above mean sea level. Soils in and around Bushland are classified as slowly permeable Pullman clay loam. The major crops in the region are corn, sorghum, winter wheat, and cotton. Wind direction is predominantly from the south/southwest direction. Annual average precipitation is about 562 mm while about 670 mm of water are needed to grow cotton. Although, only 280 mm of water (depth) fall as precipitation during the cotton growing season, New (2005).

Eddy covariance

Eddy covariance is based on the direct turbulent measurements of the product of vertical velocity fluctuations ($w'$) and a scalar (e.g. air temperature, water vapor, carbon dioxide, horizontal wind speed, etc.) concentration fluctuation ($c'$) producing a direct measurement of $H$, LE, CO$_2$, and momentum (shear forces) fluxes respectively; under the assumption that the mean vertical
velocity is zero, i.e. if turbulence is treated as a set of fluctuations about a mean value, which is called Reynolds averaging, then the value of any variable at a given time is the sum of a temporal mean (over some time period) plus an instantaneous deviation. EC principles and history can be found in Hipps and Kustas (2001), and Shuttleworth (2007) respectively. Burba and Anderson (2007) provide an on-line guidelines for EC method installation, use, maintenance, data post-processing, etc.

Two identical eddy covariance (EC) systems were installed on the East weighing lysimeter experimental fields managed under irrigation (a NE field and a SE field; Fig. 1), [4.7 ha each, i.e. 210 m wide (East-West) × 225 m long (North-South)], close to the center of the field and downwind of the predominant wind direction. Cotton was planted on May 21, 2008, on these East fields; and these fields started being irrigated (Lateral Move) on May 23. The NE field had N-S row orientation while the SE field had E-W row orientation like all prior Bushland ET research. Each EC system consisted of a fast response 3D sonic anemometer (model CSAT3, Campbell Scientific Inc., Logan, UT), a fast response open path infrared gas (H₂O and CO₂) analyzer (model LI-7500, LI-COR Inc., Lincoln, NE), a fine wire thermocouple (model FW05, Campbell Scientific Inc., Logan, UT), an air temperature/humidity sensor (model HMP45C, Vaisala Inc., Woburn, MA), and a micrologger (model CR3000, Campbell Scientific Inc., Logan, UT). A constant air density measured as the mean for each 15-min period was used (model CS106, Vaisala PTB110 barometer, Campbell Scientific, Logan, UT) to compute the flux terms.
The EC system measured turbulent fluxes at a 20-Hz frequency (20 measurements per second) and 15-min average LE and H fluxes were computed. Both EC systems were installed at a 2.5 m height above ground level. The CSAT3 sensor was oriented towards the predominant wind direction, with an azimuth angle of 225 degree from true North. The magnetic declination angle was taken into account in the EC program.

Figure 1. Three-band false color composite reflectance image, DOY 178, showing location of eddy covariance towers (circles) and grass reference weather station (square).
Airborne Remote Sensing Data

The Utah State University (USU) airborne digital multispectral system was used to acquire multispectral remote sensing data at 1-m spatial resolution for visible and near-infrared, and 4-m for thermal-infrared portions of the electromagnetic spectrum. This is a third generation of the system originally described by Neale and Crowther (1994), based on digital frame cameras but following similar image calibration procedures. The USU multispectral system comprises of three Kodak\textsuperscript{3} Megaplus digital frame cameras with interference filters centered in the green (Gn) (0.545-0.560 $\mu$m), red (R) (0.665-0.680 $\mu$m), and near-infrared (NIR) (0.795-0.809 $\mu$m) portions of the electromagnetic spectrum. The fourth camera is an Inframetrics 760 thermal-infrared (TIR) scanner (8-12 $\mu$m) that provides imagery to obtain surface radiometric temperature images.

Two airborne remote sensing images/scenes were used; each acquired over the CPRL on June 26 (DOY 178), and July 28 (DOY 210), respectively. All images were acquired close to 11:30 a.m. CST to coincide with Landsat 5 TM or ASTER satellite overpasses. These images were calibrated and transformed into surface reflectance and temperature images to be used for the estimation of reflected outgoing short wave and long wave radiation, respectively, with both components required in the estimation of spatially distributed net radiation.

\textsuperscript{3}The mention of trade names of commercial products in this article is solely for the purpose of providing specific information and does not imply recommendation or endorsement by the U.S. Department of Agriculture.
Two source energy balance model

To derive LE (or ET) Eq. 1 is solved for LE, i.e., as a residual of the surface EB equation (Brown and Rosenberg, 1973; and Stone and Horton, 1974):

\[ R_n = G + H + LE \]

where, \( R_n \) is net radiation, \( G \) is the soil heat flux, and \( H \) is sensible heat flux. Units in Eq. 1 are all in W m\(^{-2}\); with \( R_n \) positive toward the crop surface and other terms positive away from the crop surface. The conversion of LE to ET as an hourly and daily rate is detailed in the appendix.

This EB model mainly needs, remotely sensed radiometric surface temperature (\( T_{sfc} \), K), air temperature (\( T_a \), K), horizontal wind speed (\( U \), m s\(^{-1}\)), leaf area index (LAI, m\(^2\) m\(^{-2}\)), vegetation fraction cover (\( f_c \)), fraction of LAI that is green (\( f_g \)), crop height (\( h_c \), m), average leaf width (\( w \), m), and net radiation (\( R_n \)) as input. The remote sensing input dependent variables, among others, are \( T_{sfc} \), LAI, \( h_c \), \( f_c \), surface albedo, etc. In addition, the model needs weather data such as air temperature, horizontal wind speed, incoming short wave solar radiation, and relative humidity values; which were taken from the ARS weather station (ARS-Bushland, square symbol in Fig. 1) at Bushland, TX.

The TSM algorithm solves Eq. 1 for LE after finding separately the canopy \( R_n \) and \( H \) and the soil \( R_n \), \( G \) and \( H \) components, i.e. the TSM partitions each of the surface energy balance components into fluxes generated from the
vegetation canopy (first source) and the bare soil/background soil (second source) as depicted in Fig. 2. For instance, the ensemble H was estimated by summing sensible heat fluxes from both soil \( (H_s) \) and canopy \( (H_c) \). \( H_s \) occurs between the soil surface and a point above the canopy \( (Z_h) \) where air temperature \( (T_a) \) is measured; while \( H_c \) is generated between the vegetation canopy and a parcel of air at \( Z_h \), assuming a parallel resistance network (Fig. 2).

Mathematically \( H \) is expressed as:

\[
H = H_c + H_s \tag{2}
\]

\[
H_c = \frac{\rho_a C_p a (T_c - T_a)}{r_{ah}} \tag{3}
\]

\[
H_s = \frac{\rho_a C_p a (T_s - T_a)}{r_{ah} r_s} \tag{4}
\]

Figure 2. TSM parallel resistance network scheme.
\[ r_s = \frac{1}{0.004 + (0.012 U_s)} \]  

where, \( T_c \) is canopy temperature (K), \( T_s \) is soil temperature (K), \( r_s \) is the resistance to heat flow above the soil (s m\(^{-1}\)), \( r_{ah} \) is the surface aerodynamic resistance (s m\(^{-1}\)) to heat transfer, \( U_s \) is horizontal wind speed (m s\(^{-1}\)) just above the soil surface, \( \rho_a \) is air density (kg m\(^{-3}\)), and \( C_{pa} \) is specific heat of dry air (1,004 J kg\(^{-1}\) K\(^{-1}\)). \( T_c \) and \( T_s \) were estimated using Eq. 6 for a Nadir looking thermal infrared remote sensor as:

\[ T_{sfc} = \left[ f_c \times T_c^4 + (1 - f_c) \times T_c^4 \right]^{1/4} \]  

where, \( T_{sfc} \) is the so-called “ensemble (or composite) radiometric surface temperature,” and \( f_c \) is the fractional vegetation cover (function of LAI). First, to obtain \( H \), an initial estimation of \( H_c \), applying the Priestley and Taylor (1972) ET model, is performed. Subsequently, the \( H_c \) value is used to derive an initial \( T_c \) value by inverting Eq. 3 assuming a neutral atmospheric stability condition. Next, Eq. 6 is solved for \( T_s \) and updated values of \( H_c \) and \( H_s \) are computed correcting \( r_{ah} \) for atmospheric stability using the Monin-Obukhov (MO) atmospheric stability length scale (similarity theory, Foken, 2006). The MO mechanism is explained in detail in Chávez et al. (2005). \( T_c \) and \( T_s \) were verified by testing the estimated LE for a negative value, in which case temperatures are not correct, and then the soil is assumed to have a dry surface. A new iteration cycle is needed, in which LE is set to zero for the soil component and \( H_s \) is re-calculated. A new \( T_s \) and \( T_c \)
values are found and sensible heat flux components are again estimated, and canopy LE computed. In this parallel resistances network, $r_{ah}$ was eliminated from the computation of $H_s$ considering it may yield better $H_s$ ($H$) estimates for sparser vegetation according to Chávez et al. (2008).

Soil heat flux ($G$, in W m$^{-2}$) was estimated using three different methods because different remote sensing based $G$ models are developed under different conditions, i.e. crop type, soil background, soil/vegetation moisture levels, etc; thus there was the need to find a suitable $G$ model that would yield accurate values for the cotton fields under the conditions encountered in the CPRL. The first model used was that (Eq. 7) developed by Chávez et al. (2005). A second model was from Norman et al. (1995), who estimated $G$ as a function of the net radiation at the soil surface only (Eq. 8).

$$G = \left(0.3324 - 0.024 \text{LAI}\right) \times \left(0.8155 - 0.3032 \ln[\text{LAI}]\right) \times R_n$$ \hspace{1cm} (7)$$

where LAI is leaf area index ($\text{m}^2 \text{m}^{-2}$). The $G$ model is valid for the range of LAI values between 0.3 and 5.0 $\text{m}^2 \text{m}^{-2}$. This $G$ model is a combination of linear-logarithmic functions and was developed using measured data on corn and soybean fields near Ames, Iowa, and airborne remote sensing based LAI and $R_n$ estimates.

$$G = 0.35 \times R_{n_{\text{soil}}}$$ \hspace{1cm} (8)$$

where $R_{n_{\text{soil}}}$ (W m$^{-2}$) is the net radiation at the soil surface (soil only) in W m$^{-2}$. 
Also, the G model developed by Bastiaanssen (2000) was applied (Eq. 9). This model was developed using a wide variety of soil vegetation cover types.

\[
G = \frac{1}{T_B (0.0038 + 0.0074 \alpha) \times (1 - 0.98 \text{NDVI}^4)} \times \text{R}_n
\]  

(9)

where \( T_B \) (°C) is remotely sensed brightness (at sensor) surface temperature, i.e. the resulting temperature from converting the remote sensing thermal band digital numbers to radiance (system calibration) and then to temperature (Planck’s law) without any further atmospheric interference calibration. NDVI is the normalized difference vegetation index; which is determined using reflectance values from the red (R) and near-infrared (NIR) bands. Surface albedo (\( \alpha \)) was computed according to Brest and Goward (1987) as a function of R and NIR.

**Heat flux source area (footprint) model**

In an effort to understand and define the upwind area that contributes with heat fluxes to eddy covariance (or Bowen ratio) system ‘flux area source’ or footprint (FTP) models have been developed. The footprint models determine what area upwind of towers is contributing with heat fluxes to the sensors, as well as the relative weight of each particular cell (sub-area) inside the footprint limits. Different footprint models have been proposed, one-dimensional (1D), and two-dimensional (2D) models. These models are the analytical solution to the diffusion-dispersion-advection equation (Horst and Weil, 1992 and 1994). Other models are Lagrangian (Leclerc and Thurtel, 1990). Studies using these models
were able to prove that depending on the height of the vegetation, height of the instrumentation, wind speed, wind direction standard deviation, and atmospheric stability condition the shape and length of the footprint would vary upwind of the instruments, as well as the relative weights (magnitude of contribution), in each individual cell/area inside the footprint. Areas very close to the station contribute less to the total flux sensed by the instrument, areas further away (upwind) increasingly contribute more, up to a point where a peak is reached, thereafter the contribution decreases rapidly further upwind from the station (Verma, 1998). Similar behavior describes the crosswind flux distribution detected by the instruments.

In this study the FSAM (Flux Source Area Model) by Schmid (1994) was used to integrate and weight the TSM estimate ET values. The FSAM was based on the Horst and Weil (1992) model (coded in Fortran) generates the FTP weights for the source area and the approximate dimensions of the FTP area for an area that contributes up to 90% of the sensed fluxes by the instrumentation. It includes the crosswind-integrated flux as Horst and Weil (1992, 1994).

\[
F(x, y, Z_m) = D_y(x, y) F^y(x, Z_m)
\]  

where, \( F(x,y,Z_m) \) is the footprint weight function, \( D_y(x,y) \) is the cross-wind distribution function, and \( F^y(x,Z_m) \) is the cross-wind integrated function.
Results and Discussion

During DOY 178, the weather conditions were such, relative humidity (RH) was low and wind speed (H) was high, that the grass reference ET resulted in high rates (Table 1). Incoming short wave solar radiation ($R_s$) was slightly higher for DOY 178. However, on DOY 210, RH was higher and U lower thus $E_T$ was lower than on DOY 178. Further weather and crop parameter values can be found in Table 1 below. In this table note the difference in crop height ($h_c$) and leaf area index (LAI) for both DOYs. Wind direction (U dir) was from the south southwest direction; the direction of predominant winds.

Table 1. Weather and crop conditions on DOY 178 and 210.

<table>
<thead>
<tr>
<th></th>
<th>DOY</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>178</td>
</tr>
<tr>
<td>$R_s$, W m$^{-2}$</td>
<td>980</td>
</tr>
<tr>
<td>$T_a$, °C</td>
<td>31.6</td>
</tr>
<tr>
<td>RH, %</td>
<td>31</td>
</tr>
<tr>
<td>U, m s$^{-1}$</td>
<td>7.6</td>
</tr>
<tr>
<td>U dir, °</td>
<td>206</td>
</tr>
<tr>
<td>U dir std, °</td>
<td>20</td>
</tr>
<tr>
<td>$h_c$, m</td>
<td>0.18</td>
</tr>
<tr>
<td>LAI, m$^2$ m$^{-2}$</td>
<td>0.1</td>
</tr>
<tr>
<td>$E_T$, mm d$^{-1}$</td>
<td>10</td>
</tr>
</tbody>
</table>
In the process of correcting the surface aerodynamic temperature for atmospheric stability, the Monin-Obukhov stability length was computed (L), shown in Table 2. This parameter was also used in the FSAM footprint (FTP) to determine the extent of the FTP and the individual cell weight value within the boundary of the FTP. It worth noting that L was considerably large on DOY 210, which indicates that H was very small, consequently the cotton field was using most of the available energy (R_n – G) for the evapotranspiration process instead of for heating the air. Another terms used in the FTP model was the EC sensors’ height (Z_m) and the friction velocity (u’), Table 2, which was measured by the eddy covariance system.

Table 2. Variables and parameters used in the footprint FSAM.

<table>
<thead>
<tr>
<th>DOY</th>
<th>u*, m s⁻¹</th>
<th>r_ah, s m⁻¹</th>
<th>L, m</th>
<th>Z_m, m</th>
</tr>
</thead>
<tbody>
<tr>
<td>178</td>
<td>0.48</td>
<td>34.5</td>
<td>-65.2</td>
<td>2.5</td>
</tr>
<tr>
<td>210</td>
<td>0.53</td>
<td>25.5</td>
<td>-1071.5</td>
<td>2.5</td>
</tr>
</tbody>
</table>

According to the FSAM, for DOY 178, 90% of the upwind FTP length (fetch) was 84 m and the crosswind length was only 13 m. The leading edge of the FTP started about 6 m (upwind) from the EC tower location. Even though the footprint dimensions were generated for 90% of the fetch, the weights integrated under the FTP function added up to 1, i.e. accounting for 100% of the weights. In the case of DOY 210 weather/crop conditions, the FTP fetch was a little bit longer, 105 m, and the crosswind extent was 17 m (not much wind direction
variability), with the leading edge stating at 10 m from the EC tower. A graphical representation of the FTPs, for DOY 178 and 210, can be seen in Figure 3 (a) and (b), respectively. Note the effect of the stronger wind speed of DOY 178 in the FTP extent, i.e. small size. Figure 3 also shows the relative weights generated inside the FTP boundary. These weights were used to integrate the remote sensing based TSM ET estimation for comparison to the EC-based ET measurements. The ET weighting and integration procedure followed was that developed by Chávez (2005) and Chávez et al. (2005).

After generating the FTP weights, their text file was converted into an image. Subsequently, the weights image was geo-referenced (rectified) to the same coordinate system/projection/datum (UTM, m) as the reflectance/thermal imagery considering the FTP dimensions and leading edge from the EC tower location as well as the upwind wind direction.

Figure 4 depicts the superposition of the geo-rectified FTP weights image (black and white rectangles) over false color reflectance images of DOYs 178 and 210 respectively (two different days same northeast and southwest fields). The white color in the FTP image represents the concentration of larger (heavy) weights. Multiplying the geo-rectified FTP weights image by the TSM estimated ET image (ET map, Figs. 5 and 6) one obtains the FTP weighted ET values. These values were extracted from the image attribute tables and integrated according to the image pixel value histogram.
Figure 3. FSAM 3D footprint representation for DOY 178 (a) and 210 (b).
In the process of obtaining ET using the TSM, radiometric surface temperature values were partitioned into canopy (\(T_c\)) and background soil temperatures (\(T_s\)) using the modification in the calculation of the sensible heat flux originated from the soil. Results from the TSM ensemble surface temperature were reported in Table 3. These temperature values (Table 3) were
used in the estimation of the composite sensible heat flux reported in Table 4. During DOY 178, the soil temperature was about 10°C warmer than the canopy temperature, while on DOY 210 this difference was only 2°C for the NE cotton field and almost 4°C for the SE field. The much lower soil temperatures of DOY 210 were due to the higher biomass and greater ground cover presence (Table 1) on this day, even though solar radiation \( R_s \), Table 1) was slightly higher on DOY 178.

Table 3. Canopy and soil temperature from radiometric surface temperature.

<table>
<thead>
<tr>
<th>DOY</th>
<th>Site</th>
<th>( T_{sfc}, ^\circ \text{C} )</th>
<th>( T_c, ^\circ \text{C} )</th>
<th>( T_s, ^\circ \text{C} )</th>
</tr>
</thead>
<tbody>
<tr>
<td>178</td>
<td>NE</td>
<td>42.2</td>
<td>31.6</td>
<td>42.6</td>
</tr>
<tr>
<td>178</td>
<td>SE</td>
<td>41.6</td>
<td>31.5</td>
<td>41.9</td>
</tr>
<tr>
<td>210</td>
<td>NE</td>
<td>29.2</td>
<td>30.5</td>
<td>32.5</td>
</tr>
<tr>
<td>210</td>
<td>SE</td>
<td>30.9</td>
<td>30.6</td>
<td>34.4</td>
</tr>
</tbody>
</table>

As previously discussed above, \( H \) resulted very low during DOY 210 (Table 4), lower for NE cotton field than for the SE field; an indication of higher ET rate at the NE field. In contrast \( H \) was very high during DOY 178, which indicates that the available energy was used to heat the air and the soil since the cotton plants were very short with not much biomass and probably due to limited soil water content. The resulting \( H \) was somewhat over estimated by the modified TSM algorithm. Sensible heat flux estimation error was 15 W m\(^{-2}\) (standard deviation, \( \sigma_d \), of 15.7 W m\(^{-2}\)), i.e. an error of 17.2 ± 15.5%. This \( H \) result is an indication of good canopy and soil temperature partitioning.
Soil heat flux was better estimated by the Bastiaanssen’s model in a comparison with measured G by soil heat flux plates (accounting for heat storage). Bastiaanssen’s model predicted G with an average error of only -9.9 W m\(^{-2}\) (\(\sigma_d\) of 20.2 W m\(^{-2}\)). In percent based on mean values these were -7.1% average error with a \(\sigma_d\) of 13.6%; while Chávez et al. (2005) model produced G estimates with large errors, in the order of 100%. This result was somewhat expected since the former was developed for a wider range of crops (including cotton), while the latter was developed using measured G values obtained on corn and soybean fields. In the case of the third G model, the errors were 46.6% in average, with a \(\sigma_d\) of 30.1%, thus not suitable for this study. Therefore, Bastiaanssen’s G model was used in the TSM applied in this research. Soil heat flux values, using Bastiaanssen’s model, can be found in Table 4, for individual fields and DOYs.

Net radiation was estimated accurately by the TSM, the average estimation error was only 39.8 W m\(^{-2}\) (\(\sigma_d\) of 7.9 W m\(^{-2}\)), or in percent 6.5 \(\pm\) 1.6%. Table 4 shows the individual net radiation values for each DOY and field location.

Evapotranspiration, according to the FTP integrated TSM estimation, doubled on DOY 210 with respect to the ET rate of DOY 178 (Table 4). In addition, when the TSM ET values of Table 4 were compared to values measured by the EC systems it turned out that the TSM slightly under predicted ET by 0.5 mm d\(^{-1}\) (std of 0.6 mm d\(^{-1}\)), or by 5.1 \(\pm\) 7.2%, respectively. This under prediction is relatively small if one considers that the uncertainty associated with the instrumentation, (for each term of the energy balance) in general ranges from
10-20%. Moreover, ET was better predicted than when a satellite image was used and no modification was made on the TSM for the calculation of \( H \); in which case ET resulted in an under prediction error of 0.8 mm d\(^{-1}\) (std of 0.8 mm d\(^{-1}\)), or by \( 9.2 \pm 9.0\% \) respectively, Chávez et al. (2007). It is important to have in mind that in the latter case no footprint model was used and the pixel resolution was coarser.

This result was evidence that the modification proposed in Chávez et al. (2008) for the TSM to estimate \( H \) for the ground, under sparse/low biomass levels, is appropriate. Furthermore, the FSAM footprint seems to be a viable means to weight/integrate very high spatial resolution ET map pixels.

Table 4. Net radiation, soil/sensible heat flux and ET estimated by the TSM.

<table>
<thead>
<tr>
<th>DOY/Site</th>
<th>178/NE</th>
<th>178/SE</th>
<th>210/NE</th>
<th>210/SE</th>
</tr>
</thead>
<tbody>
<tr>
<td>( R_n ) W m(^{-2})</td>
<td>625.9</td>
<td>619.7</td>
<td>719.9</td>
<td>690.4</td>
</tr>
<tr>
<td>( G ) W m(^{-2})</td>
<td>109.3</td>
<td>114.6</td>
<td>73.1</td>
<td>78.1</td>
</tr>
<tr>
<td>( H ) W m(^{-2})</td>
<td>261.8</td>
<td>247.2</td>
<td>17.0</td>
<td>24.0</td>
</tr>
<tr>
<td>ET, mm d(^{-1})</td>
<td>4.1</td>
<td>4.2</td>
<td>8.9</td>
<td>8.2</td>
</tr>
</tbody>
</table>

Finally, maps of distributed ET are shown in Figures 5 and 6 for DOY 178 and 210 respectively. As per the distributed ET values in both Figs., the NE cotton field showed more ET heterogeneity (variability) for DOY 178 than for DOY 210. Also, Figure 5 shows the SE field bordering with a much drier fallow winter wheat field; which could have been an issue had the wind speed been calm because the heat flux source area would have extended into the drier fallow
land, thus resulting in a probable lower ET measurement by the eddy covariance system.

Figure 5. Map of distributed ET generated with the TSM for DOY 178
Figure 6. Map of distributed ET generated with the TSM for DOY 210
CONCLUSION

A modified two source energy balance model was applied to very high resolution airborne multispectral imagery to generate distributed ET values. And a 2D heat flux footprint model was used to weight and integrate the resulting ET values.

Results indicated that the modification proposed by Chávez et al. (2008) for the TSM sensible heat flux estimation originating from the ground (substrate), under sparse/low biomass levels, was appropriate. Furthermore, the FSAM footprint seems to be a viable means to weight/integrate very high spatial resolution ET map pixels.

In addition, soil heat flux needs to be estimated by a remote sensing-based model that is valid for the vegetation/background conditions encountered during the scene (image) acquisition. In other words, a soil heat flux model is needed which had been developed considering (is valid for) a wide range of crops, crop biomass level (range of LAI values), soil water content levels, sun zenith angle and sensor bandwidths.

Further research will include the incorporation of a number of airborne scenes to test the modified TSM under dense biomass presence where the resistance network modification suggests ignoring the sensible heat flux originated from the substrate when LAI is larger than 3 m² m⁻².
REFERENCES


**APPENDIX**

**LE Conversion into ET Rates**

Once the TSM has produced estimates of latent heat fluxes (LE, W m\(^{-2}\)), these need to be converted into an equivalent water depth or instantaneous ET rates (\(\text{ET}_i\), mm h\(^{-1}\)).

LE is converted into ET as follows:

\[
\text{ET}_i = \frac{3,600 \times \text{LE}}{\lambda_{\text{LE}} \times \rho_w}
\]

(11)

where, \(\text{ET}_i\) is hourly ET (mm h\(^{-1}\)) calculated from the TSM estimated instantaneous LE (W m\(^{-2}\)). \(\lambda_{\text{LE}}\) is the latent heat of vaporization (MJ kg\(^{-1}\)), equal to (2.501 – 0.00236 \(T_a\)), being \(T_a\) in ° C units, and \(\rho_w\) is water density (~ 1 Mg m\(^{-3}\)).

The 3,600 number is a factor to time conversion of s h\(^{-1}\).

In addition, daily evapotranspiration (\(\text{ET}_d\)) was computed as:

\[
\text{ET}_d = \left( \frac{\text{ET}_i}{\text{ET}_o} \right) \times \text{ET}_o
\]

(12)

where, \(\text{ET}_{oi}\) is hourly grass reference ET (mm h\(^{-1}\)), calculated using the ARS-Bushland weather station hourly data and the ASCE-EWRI (2005) standardized Penman-Monteith method. \(\text{ET}_o\) is the daily ET (mm d\(^{-1}\)) computed by adding up the hourly ET over the course of the entire day; and \(\text{ET}_i\) is the TSM estimated actual crop instantaneous ET (mm h\(^{-1}\)) values.